

## SIMULATION AND ANALYSIS OF PARABOLOID SOLAR CONCENTRATORS: A PYTHON-BASED APPROACH FOR VISUALIZING RAY TRACING AND PERFORMANCE

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**Abstract:** Paraboloid solar concentrators (PSCs) are highly efficient devices used for concentrating solar energy onto a focal point, which can then be utilized for thermal energy collection. The efficiency of a PSC is heavily influenced by its geometric design, particularly the parabolic dish, which focuses parallel rays of sunlight onto a receiver. This paper presents a simulation-based approach to model the geometry and ray tracing of a parabolic solar concentrator. Using fundamental physical principles, we model the parabolic surface, simulate the reflection of light rays, and visualize their convergence at the focal point. The results provide a foundation for more advanced studies on the optimization and performance of PSCs in solar thermal systems.

**Key words:** Paraboloid Solar Concentrators (PSCs), Ray Tracing, Solar Energy Concentration, Focal Point, Simulation, Python Visualization, Parabolic Geometry, Solar Thermal Systems, Reflection Law, Concentrated Solar Power (CSP).

### Introduction:

Paraboloid solar concentrators (PSCs) are widely used in solar thermal applications due to their high concentration ratios and efficient heat absorption properties. A PSC is shaped like a paraboloid of revolution, which enables it to focus incoming parallel rays of sunlight onto a single focal point. This feature makes it ideal for concentrated solar power (CSP) systems, which require high temperatures for energy generation.

The performance and efficiency of a PSC depend on several factors, including the accuracy of the geometry, the reflective surface's material properties, and the thermal dynamics of the receiver. A critical aspect of optimizing PSCs involves understanding how solar rays reflect off the parabolic dish and ensuring their accurate convergence at the focal point. This study introduces [1] a simulation-based approach to model the parabolic dish, simulate ray tracing, and visualize the process in a 3D environment using Python.

### The Parabolic Dish Geometry:

A paraboloid is mathematically described by the equation:

$$z = \frac{x^2 + y^2}{4f} \text{ where:}$$

- $f$  is the focal length of the paraboloid.
- $(x, y, z)$  are the coordinates of a point on the parabolic surface.

The geometry of the paraboloid is designed so that all incoming parallel rays of sunlight (assumed to be parallel to the z-axis in this model) are reflected toward a single focal point located along the z-axis. The parabolic shape ensures that the reflected rays converge accurately, which is crucial for efficient solar energy concentration.

The focal length  $ff$  significantly impacts the concentrator's size and efficiency, as well as its ability to focus light effectively. By understanding the geometric properties of the paraboloid, we can optimize the concentrator's design for different solar applications[2].

### Ray Tracing and Reflection:

Ray tracing is a crucial concept in understanding the operation of PSCs. In our model, rays originate from a distant light source (the Sun), and we assume they are parallel to the z-axis. These rays are simulated to reflect off the parabolic dish and converge at the focal point. The reflection of light follows the law of reflection, where the angle of incidence is equal to the angle of reflection.

In our simulation, rays are reflected from the edge of the paraboloid, with each ray's direction determined by its angle of incidence and the geometry of the surface. The model ensures that all rays, regardless of their initial direction, will ultimately converge at the receiver positioned at the focal point.

### Mathematical Model and Visualization Approach:

To model and visualize the simulation, we use Python's 3D visualization capabilities.

The simulation is divided into several key steps:

#### Step 1: Generate the Paraboloid Surface

The surface of the paraboloid is modeled using the parabolic equation, and a mesh grid is created to represent its 3D shape. The range of z-coordinates[3] is divided into discrete points, and the corresponding xx- and yy-coordinates are computed using the following equations:

$$x = \frac{z^2}{4f} \cos(\theta) \quad y = \frac{z^2}{4f} \sin(\theta)$$

where  $\theta$  is the angle in the x-y plane, and  $z$  spans the height of the paraboloid.

#### Step 2: Simulate Ray Reflection

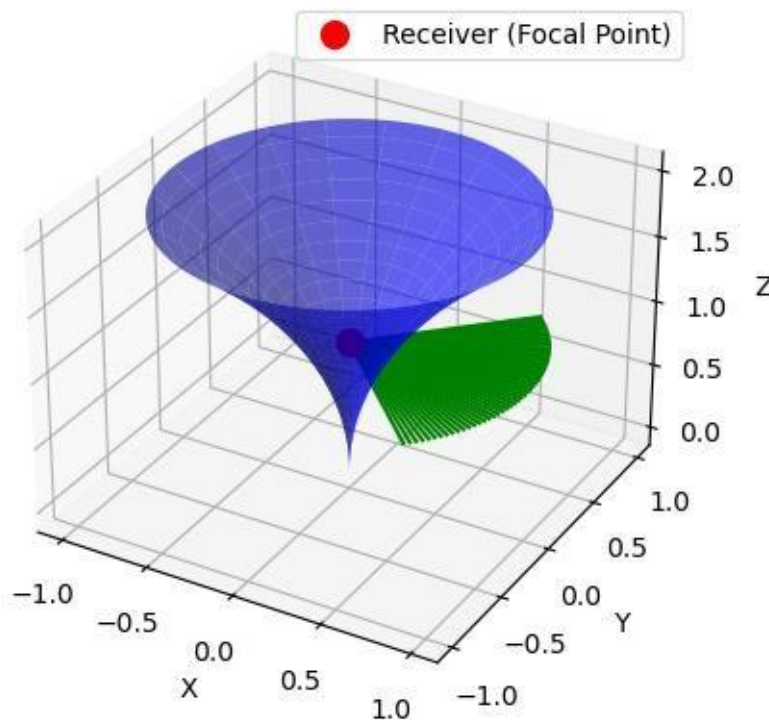
Rays are simulated to approach the parabolic surface at various angles. Each ray starts at the origin (representing a distant light source), and its direction is determined by the incident angle. Rays are then projected towards the paraboloid surface, where their reflection is calculated, ensuring that they all converge at the focal[4] point.

#### Step 3: Visualize the Results

Using Python's plotting libraries, the results are visualized in a 3D[1] plot. The parabolic surface is represented as a blue surface, and the rays are shown as green lines reflecting from the surface

towards the focal point, which is represented by a red dot. This visualization offers insights into the behavior of the rays and how the geometry of the paraboloid facilitates their convergence at the [6] receiver.

Paraboloid Solar Concentrator with Ray Tracing



### Results and Visualization:

The Python-based simulation produces a 3D plot where the following elements are visualized:

- **Paraboloid Surface:** A blue surface representing the parabolic dish.
- **Rays:** Green lines showing the rays as they reflect off the parabolic surface and converge at the focal point (shown as a red dot).
- **Receiver:** The receiver located at the focal point, where the concentrated solar energy is collected.

This visualization serves as a simplified representation of how solar energy is concentrated at the focal point. It provides an intuitive understanding of the geometry and its role in efficiently directing sunlight toward the receiver.

### Conclusion

This study demonstrates an effective and simple approach for simulating and visualizing the performance of a parabolic solar concentrator. By simulating the reflection of rays off the parabolic surface and their convergence at the receiver, we gain valuable insights into how the concentrator's geometry impacts its efficiency in focusing solar energy. The presented model offers a foundation for future research aimed at optimizing the performance of PSCs.

Future work could explore more advanced ray-tracing techniques, the incorporation of thermal efficiency models, and the impact of environmental factors, such as wind, cloud cover, and temperature variations, on the performance of PSCs. Additionally, optimizing the geometry for various CSP applications and integrating real-world environmental variables could further enhance the efficiency of solar concentrators.

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